

Modeling Cognitive Radios as a Dynamical System

- Dynamical system

- A system whose change in state is a function of the current state and time

- Autonomous system

- Not a function of time
- OK for synchronous timing

- Characteristic function

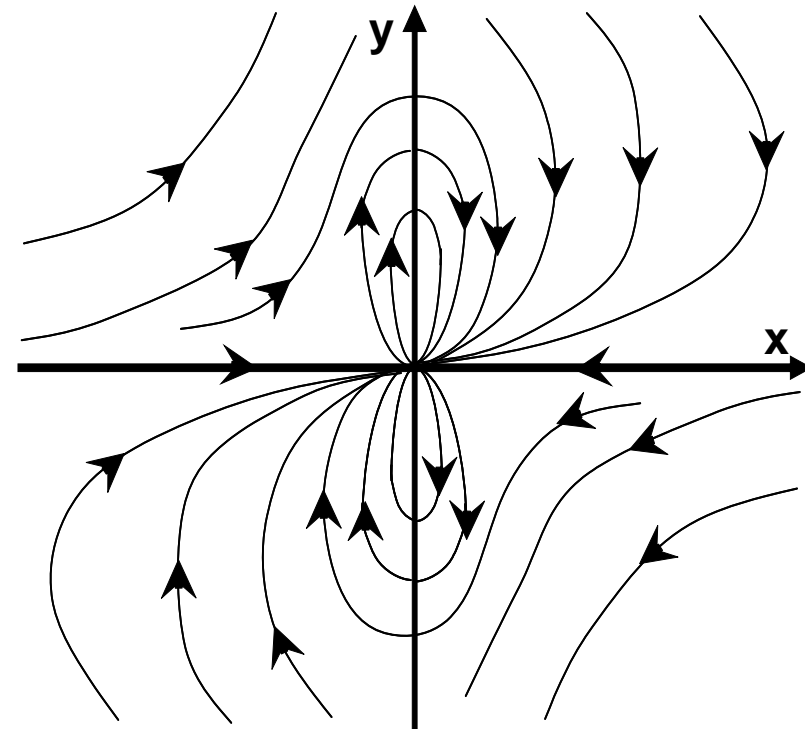
$$\dot{a} = g(a, t)$$

- Evolution function $d : A \times T \rightarrow A$

- First step in analysis of dynamical system
- Describes state as function of time & initial state.

- For simplicity $d = \times_{j \in N} d_j = d : A \rightarrow A$

while noting the relevant timing model



Optimality

- In general we assume the existence of some design objective function $J:A\rightarrow\mathbb{R}$
- The desirableness of a network state, a , is the value of $J(a)$.
- In general maximizers of J are unrelated to fixed points of d .

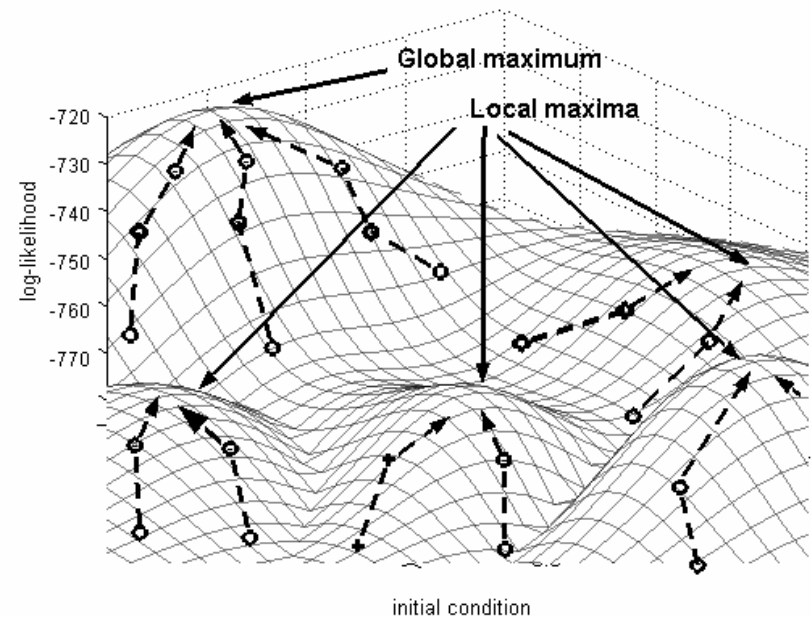
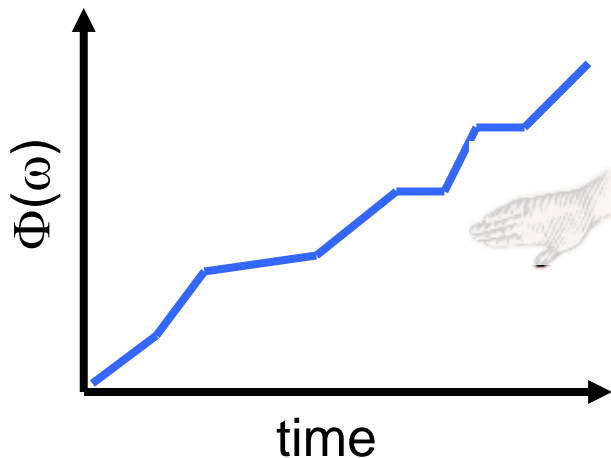
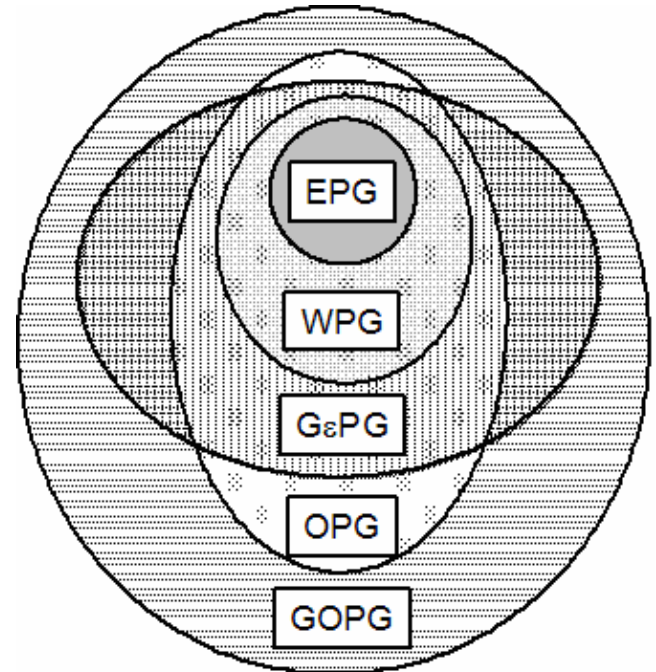


Figure from Fig 2.6 in I. Akbar, "Statistical Analysis of Wireless Systems Using Markov Models," PhD Dissertation, Virginia Tech, January 2007

Potential Games

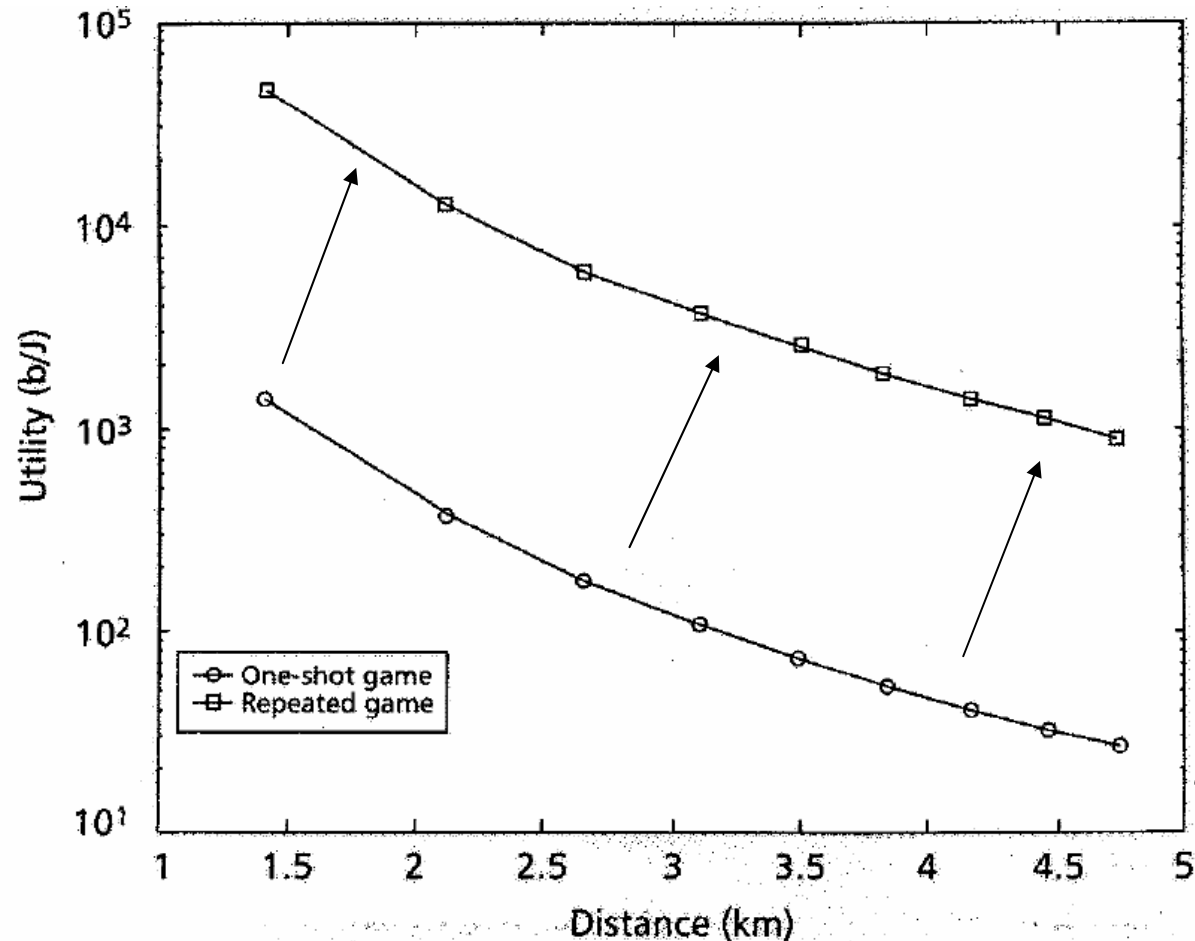
- Existence of a function (called the potential function, V), that reflects the change in utility seen by a unilaterally deviating player.
- Cognitive radio interpretation:
 - Every time a cognitive radio unilaterally adapts in a way that furthers its own goal, some real-valued function increases.



Potential Game	Relationship ($\forall i \in N, \forall a \in A$)
Exact (EPG)	$u_i(b_i, a_{-i}) - u_i(a_i, a_{-i}) = V(b_i, a_{-i}) - V(a_i, a_{-i})$
Weighted (WPG)	$u_i(b_i, a_{-i}) - u_i(a_i, a_{-i}) = \alpha_i [V(b_i, a_{-i}) - V(a_i, a_{-i})]$
Ordinal (OPG)	$u_i(b_i, a_{-i}) - u_i(a_i, a_{-i}) > 0 \Leftrightarrow V(b_i, a_{-i}) - V(a_i, a_{-i}) > 0$
Generalized Ordinal (GOPG)	$u_i(b_i, a_{-i}) - u_i(a_i, a_{-i}) > 0 \Rightarrow V(b_i, a_{-i}) - V(a_i, a_{-i}) > 0$
Generalized ε (GεPG)	$u_i(b_i, a_{-i}) > u_i(a_i, a_{-i}) + \varepsilon_1 \Rightarrow V(b_i, a_{-i}) > V(a_i, a_{-i}) + \varepsilon_2$

Improvement from Punishment

- Throughput/unit power gains be enforcing a common received power level at a base station
- Punishment by jamming
- Without benefit to deviating, players can operate at lower power level and achieve same throughput



802.11h: A simple cognitive radio

Observe

- Must estimate channel characteristics (TPC)
- Must measure spectrum (DFS)

Orientation

- a) Radar present?
- b) In band with satellite??
- c) Bad channel?
- d) Other WLANs?

Decision

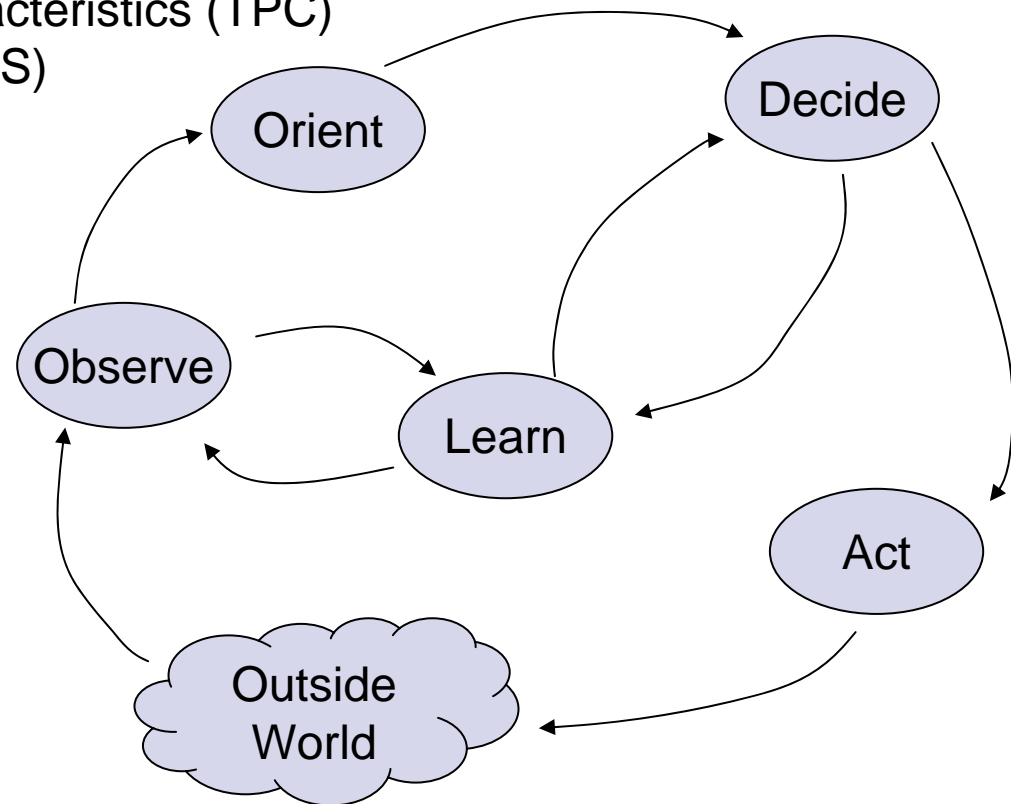
- Change frequency
- Change power
- Nothing

Action

Implement decision

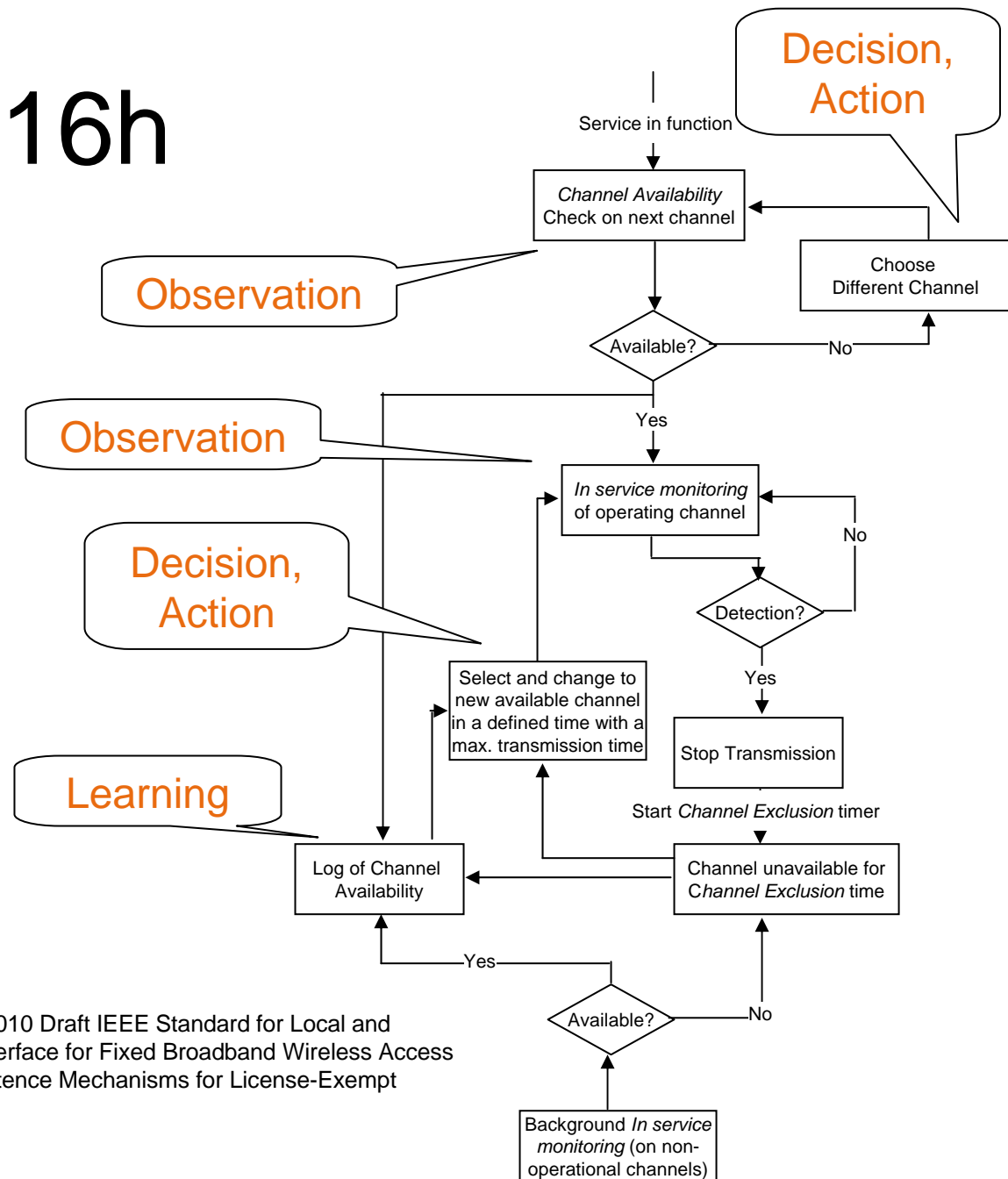
Learn

- Not in standard, but most implementations should learn the environment to address intermittent signals



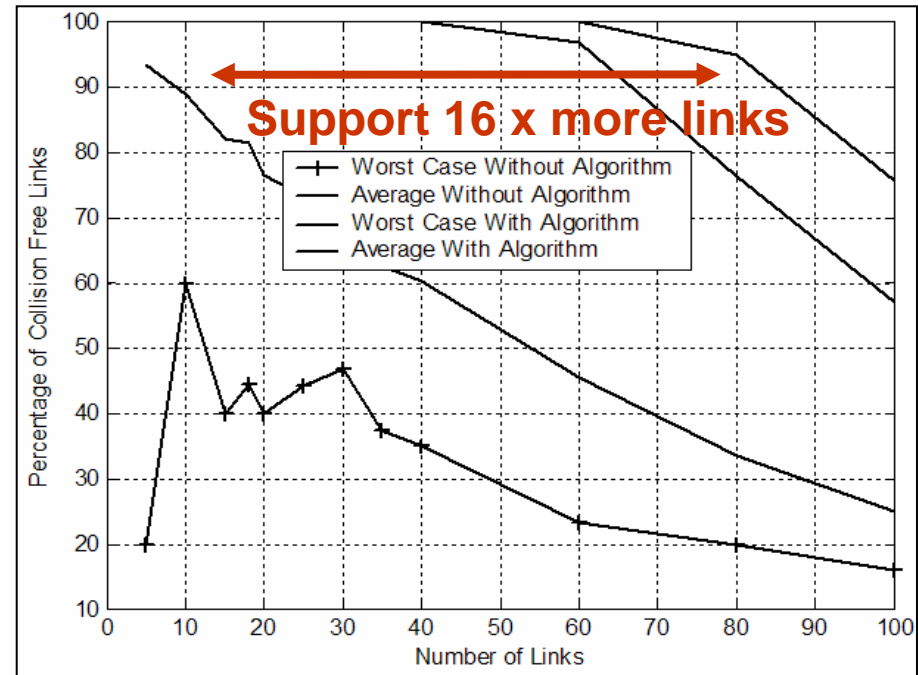
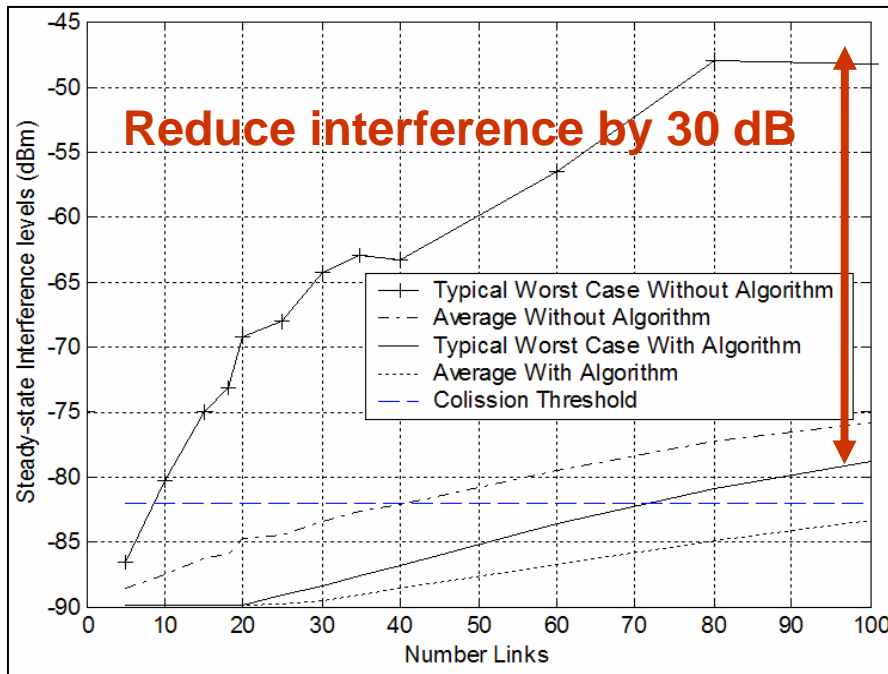
DFS in 802.16h

- Drafts of 802.16h defined a generic Dynamic Frequency Selection algorithm which implements observation, decision, action, and learning processes
- Very simple implementation



Modified from Figure h1 IEEE 802.16h-06/010 Draft IEEE Standard for Local and metropolitan area networks Part 16: Air Interface for Fixed Broadband Wireless Access Systems Amendment for Improved Coexistence Mechanisms for License-Exempt Operation, 2006-03-29

Aggregate Statistics for Peer-to-Peer Network



- Similar algorithm but cognitive decision processes span links
- No coordination between decision processes
- Localized reasoning leads to global optima
- Steady-state performance equivalent to centralized local search